

NAME

qmath - fixed-point math library based on the "Q" number format

SYNOPSIS

```
#include <sys/qmath.h>
```

DESCRIPTION

The **qmath** data types and APIs support fixed-point math based on the "Q" number format. The APIs have been built around the following data types: *s8q_t*, *u8q_t*, *s16q_t*, *u16q_t*, *s32q_t*, *u32q_t*, *s64q_t*, and *u64q_t*, which are referred to generically in the earlier API definitions as *QTYPE*. The *ITYPE* refers to the `stdint(7)` integer types. *NTYPE* is used to refer to any numeric type and is therefore a superset of *QTYPE* and *ITYPE*.

This scheme can represent Q numbers with [2, 4, 6, 8, 16, 32, 48] bits of precision after the binary radix point, depending on the *rpsht* argument to **Q_INI()**. The number of bits available for the integral component is not explicitly specified, and implicitly consumes the remaining available bits of the chosen Q data type.

Operations on Q numbers maintain the precision of their arguments. The fractional component is truncated to fit into the destination, with no rounding. None of the operations is affected by the floating-point environment.

For more details, see the *IMPLEMENTATION DETAILS* below.

LIST OF FUNCTIONS**Functions which create/initialise a Q number**

<i>Name</i>	Description
Q_INI(3)	initialise a Q number

Numeric functions which operate on two Q numbers

<i>Name</i>	Description
Q_QADDQ(3)	addition
Q_QDIVQ(3)	division
Q_QMULQ(3)	multiplication
Q_QSUBQ(3)	subtraction
Q_NORMPREC(3)	normalisation
Q_QMAXQ(3)	maximum function
Q_QMINQ(3)	minimum function
Q_QCLONEQ(3)	

identical copy

Q_QCPYVALQ(3)

representational copy

Numeric functions which apply integers to a Q number

Name Description

Q_QADDI(3) addition

Q_QDIVI(3) division

Q_QMULI(3) multiplication

Q_QSUBI(3) subtraction

Q_QFRACI(3) fraction

Q_QCPYVALI(3)

overwrite

Numeric functions which operate on a single Q number

Name Description

Q_QABS(3) absolute value

Q_Q2D(3) double representation

Q_Q2F(3) float representation

Comparison and logic functions

Name Description

Q_SIGNED(3) determine sign

Q_LTZ(3) less than zero

Q_PRECEQ(3) compare bits

Q_QLTQ(3) less than

Q_QLEQ(3) less or equal

Q_QGTQ(3) greater than

Q_QGEQ(3) greater or equal

Q_QEQ(3) equal

Q_QNEQ(3) not equal

Q_OFLOW(3) would overflow

Q_RELPREC(3)

relative precision

Functions which manipulate the control/sign data bits

Name Description

Q_SIGNSHFT(3)

sign bit position

Q_SSIGN(3) sign bit

Q_CRAWMASK(3)
control bitmask

Q_SRAWMASK(3)
sign bitmask

Q_GCRAW(3) raw control bits

Q_GCVAL(3) value of control bits

Q_SCVAL(3) set control bits

Functions which manipulate the combined integer/fractional data bits

<i>Name</i>	Description
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Q_IFRAWMASK(3)	integer/fractional bitmask
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Q_IFVALIMASK(3)	value of integer bits
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Q_IFVALFMASK(3)	value of fractional bits
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Q_GIFRAW(3)	raw integer/fractional bits
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Q_GIFABSVAL(3)	absolute value of fractional bits
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Q_GIFVAL(3)	real value of fractional bits
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Q_SIFVAL(3)	set integer/fractional bits
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Q_SIFVALS(3)	set separate integer/fractional values
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Functions which manipulate the integer data bits

<i>Name</i>	Description
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Q_IRAWMASK(3)	integer bitmask
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Q_GIRAW(3)	raw integer bits
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Q_GIABSVAL(3)	absolute value of integer bits
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Q_GIVAL(3)	real value of integer bits
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Q_SIVAL(3)	set integer bits
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Functions which manipulate the fractional data bits

<i>Name</i>	Description
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Q_FRAWMASK(3)	fractional bitmask
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Q_GFRAW(3)	raw fractional bits
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Q_GFABSVAL(3)	
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absolute value of fractional bits
 Q_GFVAL(3) real value of fractional bits
 Q_SFVAL(3) set fractional bits

Miscellaneous functions/variables

<i>Name</i>	Description
Q_NCBITS(3)	number of reserved control bits
Q_BT(3)	C data type
Q_TC(3)	casted data type
Q_NTBITS(3)	number of total bits
Q_NFCBITS(3)	number of control-encoded fractional bits
Q_MAXNFBITS(3)	number of maximum fractional bits
Q_NFBITS(3)	number of effective fractional bits
Q_NIBITS(3)	number of integer bits
Q_RPSHFT(3)	bit position of radix point
Q_ABS(3)	absolute value
Q_MAXSTRLEN(3)	number of characters to render string
Q_TOSTR(3)	render string
Q_SHL(3)	left-shifted value
Q_SHR(3)	right-shifted value
Q_DEBUG(3)	render debugging information
Q_DFV2BFV(3)	convert decimal fractional value

IMPLEMENTATION DETAILS

The **qmath** data types and APIs support fixed-point math based on the "Q" number format. This implementation uses the Q notation $Qm.n$, where m specifies the number of bits for integral data (excluding the sign bit for signed types), and n specifies the number of bits for fractional data.

The APIs have been built around the following `q_t` derived data types:

```
typedef int8_t      s8q_t;
typedef uint8_t     u8q_t;
typedef int16_t     s16q_t;
typedef uint16_t    u16q_t;
typedef int32_t     s32q_t;
typedef uint32_t    u32q_t;
```


The count of total bits is derived from the size of the `q_t` data type. For example, a `s32q_t` has 32 total bits.

The count of control-encoded fractional bits is derived from calculating the number of fractional bits per the control bit encoding scheme. For example, the control bits binary value of 101 encodes a fractional bit count of $2 \times 16 = 32$ fractional bits.

The count of maximum fractional bits is derived from the difference between the counts of total bits and control/sign bits. For example, a `s32q_t` has a maximum of $32 - 3 - 1 = 28$ fractional bits.

The count of effective fractional bits is derived from the minimum of the control-encoded fractional bits and the maximum fractional bits. For example, a `s32q_t` with 32 control-encoded fractional bits is effectively limited to 28 fractional bits.

The count of integer bits is derived from the difference between the counts of total bits and all other non-integer data bits (the sum of control, fractional and sign bits.) For example, a `s32q_t` with 8 effective fractional bits has $32 - 3 - 8 - 1 = 20$ integer bits. The count of integer bits can be zero if all available numeric data bits have been reserved for fractional data, e.g., when the number of control-encoded fractional bits is greater than or equal to the underlying Q data type's maximum fractional bits.

EXAMPLES

Calculating area of a circle with `r=4.2` and `rpsft=16`

```
u64q_t a, pi, r;
char buf[32]

Q_INI(&a, 0, 0, 16);
Q_INI(&pi, 3, 14159, 16);
Q_INI(&r, 4, 2, 16);

Q_QCLONEQ(&a, r);
Q_QMULQ(&a, r);
Q_QMULQ(&a, pi);

Q_TOSTR(a, -1, 10, buf, sizeof(buf));
printf("%s\n", buf);
```

Debugging

Declare a Q20.8 `s32q_t` number `s32`, initialise it with the fixed-point value for $5/3$, and render a debugging representation of the variable (including its full precision decimal C-string representation), to the console:

```
s32q_t s32;
Q_INI(&s32, 0, 0, 8);
Q_QFRACI(&s32, 5, 3);
char buf[Q_MAXSTRLEN(s32, 10)];
Q_TOSTR(s32, -1, 10, buf, sizeof(buf));
printf(Q_DEBUG(s32, "", "\n\ttostr=%s\n", 0), buf);
```

The above code outputs the following to the console:

```
"s32"@0x7ffffffe7d4
    type=s32q_t, Qm.n=Q20.8, rpsht=11, imin=0xfff00001, \
imax=0xffff
    qraw=0x00000d53
    imask=0x7fff800, fmask=0x000007f8, cmask=0x00000007, \
ifmask=0x7ffff8
    iraw=0x00000800, iabsval=0x1, ival=0x1
    fraw=0x00000550, fabsval=0xaa, fval=0xaa
    tostr=1.664
```

Note: The "\" present in the rendered output above indicates a manual line break inserted to keep the man page within 80 columns and is not part of the actual output.

SEE ALSO

errno(2), math(3), Q_FRAWMASK(3), Q_IFRAWMASK(3), Q_INI(3), Q_IRAWMASK(3), Q_QABS(3), Q_QADDI(3), Q_QADDQ(3), Q_SIGNED(3), Q_SIGNSHFT(3), stdint(7)

HISTORY

The **qmath** functions first appeared in FreeBSD 13.0.

AUTHORS

The **qmath** functions and this manual page were written by Lawrence Stewart <lstewart@FreeBSD.org> and sponsored by Netflix, Inc.